Analysis of Edge Detection on Compressed Images with Different Complexities

Vladimir Maksimović¹, Branimir Jakšić¹, Mile Petrović¹, Petar Spalević¹, Mirko Milošević²

¹ Faculty of Technical Sciences, University of Pristina in Kosovska Mitrovica, Knjaza Milosa 7, 38220 Kosovska Mitrovica, Serbia, vladimir.maksimovic@pr.ac.rs, branimir.jaksic@pr.ac.rs, mile.petrovic@pr.ac.rs, petar.spalevic@pr.ac.rs, mirko.milosevic@viser.edu.rs

²School of Electrical and Computer Engineering of Applied Studies, Vojvode Stepe 283, 11000 Belgrade, Serbia

Abstract: This paper provides edge detection analysis on images, which consist of different numbers of details (small, medium and high number of details) and which are compressed by different compression algorithms - JPEG, JPEG2000 and SPIHT. Images from the BSD (Berkeley Segmentation Database) database were used and compressed with different number of bits per pixel. The analysis was performed for five edge detectors: Canny, LoG, Sobel, Prewitt, and Roberts. The fidelity of the detected edges was determined using the objective measures Figure of Merit (FOM), F measure and Performance Ratio (PR), where the reference value was taken from the GroundTruth image. Based on the results presented in the tables, it can be concluded that edge detection behaves differently depending on the number of bits per pixel and applied compression algorithm, as well as, the number of details in the image. Roberts operator has been proven to be the best solution, when it is necessary to perform better edge detection over compressed images with small a number of details, but Canny shows better results for images with a high number of details.

Keywords: edge detection; compression; image processing; Figure of Merit (FOM); F measure; Performance Ratio (PR); image complexity; bit per pixel (BPP)

1 Introduction

In today's multimedia systems, it is almost impossible to find a system that does not use image, video or audio compression. However, the development of technology has also brought an increasing use and processing of images, from use in daily life to those more serious professional uses such as image analysis in medicine, sensor networks, smart and security systems, television and so on. An uncompressed image requires more storage space for storage and processing, as well as, transmission via telecommunication channels. Considering this fact, there is a great deal of interest among researchers regarding image processing and compression. The size of the image can be large so that it is very impractical to store or transfer, especially when it comes to real-time image processing systems. For this reason, many image compression methods have been developed, but we can divide them all into lossy and lossless ones [1-3].

Depending on the need, various compression techniques and compression algorithms are applied, and as a result, the most popular are JPEG and JPEG2000. JPEG standard compression is based on Discrete Cosine Transform (DCT), while JPEG2000 compression is based on Discrete Wavelet Transform (DWT) [4-9]. Also, the compression algorithm based on Embedded Zero Tree Wavelet (EZW) is the SPIHT algorithm [10-12]. As mentioned, compression and coding techniques are used in many systems, i.e. where image processing is performed, so there are techniques for medical images [13-17], radar images [18-20], satellite images [21-23] and for many other smart systems combining different compression and coding techniques [24-26]. Image processing is an integral part of machine learning and artificial intelligence, where there are classifiers and neural network models that can be used as in [27], [28]. Also, the mathematical models presented in [29], [30] provide ideas for improving the algorithms for estimating image complexity used in this paper.

We are also witnessing an increase in the use of smart networks, the use of artificial intelligence to analyze, collect and process data. Such systems are mainly based on image processing and data processing, where the main processes are the extraction of a particular object from the scene, where edge detection and segmentation play an important role [31-34]. However, all of this gain particular weight and interest with the emergence and implementation of such systems on devices like Raspberry Pi and Arduino, which very often use real-time image processing, object detection and segmentation [35-39]. Many techniques and enhancements have been proposed to maximize the quality of edge detection and segmentation [39-43]. Given that the resolutions and image quality are increasing, thus occupying a large storage space, it is important to do compression so as not to impair the quality. Compression will affect edge detection, as examined in [44] using a wavelet transform, which underlies some compression algorithms, as well as facial recognition [45-47]. Therefore, the effect of compression on edge detection is presented in [44] where the authors examined only the influence of wavelet-based compression. The authors in [45-47] examined the effect of compression on face recognition using the JPEG and JPEG2000 algorithms, while the effect on edge detection was not examined. In this paper, the idea is to examine the impact of compression on edge detection using the most common compression algorithms.

The rest of the paper is divided as follows: Section 2 explains the system model, that is, the basic setting on which a detailed edge detection analysis was made. The images that were used for analysis are given, followed by tabulated values

obtained during compression using different algorithms. In this section can be seen the method used by the authors to perform the analysis. Section 3 presents the obtained results of edge detection for five edge detectors over compressed images using different compression algorithms. The tables show three objective measures, and based on the results the discussion was made. In Section 3, there are sub sections for each operator. Finally, the conclusion of this paper is given, as well as the direction of future research.

2 System Model

This paper analysis the impact of JPEG, JPEG2000, and SPIHT algorithm on edge detection, where images are compressed with different number of bits per pixel (BPP), namely: 0.1, 0.3, 0.5, 1, 1.5, and 3 BPP. Images from the BSD. Used images are from the BSD database with the corresponding GroundTruth [48]. The images were selected to meet the three complexity criteria of small, medium and high complexity [49], that is, each image consists of a different level of detail: small, medium, and high level of details [49]. Table 1 shows the obtained values on the basis of which are the selected images from the database BSD, which meet the defined criteria.

Complexity in an image shows information about how much details exists in that image, and this can be observed for both static images and video formats. The simplest way of determining complexity is on the basis of observer's visual assessment. However, it is not an objective measure to confirm the credibility of that assessment [50-52]. Since this paper looks at the effect of compression on edge detection, there are also methods that measure image complexity based on compression and thus make a link between compression, quality and complexity. One way of doing this is shown in [50]. JPEG, JPEG200 and SPIHT algorithms are based on the DCT and DWT techniques, so the number of details was calculated by making DCT and DWT on the high-frequency components (details), which are divided into four quadrants, along both directions (x and y). After that, the mean absolute value of the amplitude of the components belonging to the quadrants is calculated according to [49]: DCT in quadrant 1 (DCTD); DCT in quadrants 2 and 3 (DCTM); DWT in quadrant 1 (DWT); DWT in quadrants 2 and 3 (DWTM).

Edge detection and analysis were performed on the selected and compressed images for five edge detectors, namely: Canny, LoG, Sobel, Prewitt, and Roberts. Gradient and Laplace edge detection algorithms were written in Matlab, while image compression was performed using VcDemo. So, first, the images extracted from the BSD database with the corresponding GroundTruth were selected to satisfy the criteria in [49] using the technique from that paper. After that, the images were compressed in VcDemo using JPEG, JPEG2000 and SPIHT

algorithm with different BPP. In the end, edge detection over compressed images was performed using five operators and objective measures are calculated in Matlab.

| | Images | DCTD | DCTM | WVTD | WVTM |
|-------------|---------|------|---------|---|-------|
| Culturian T | 4020011 | <2 | <3.5 | <0.8 | <1.2 |
| Criterion L | #230011 | 0.75 | 1.69 | 69 0.17 0.4 -6.5 1.4-1.8 2-2. | 0.44 |
| Cuitonian M | 1045051 | 3-4 | 4.5-6.5 | 1.4-1.8 | 2-2.8 |
| Criterion M | #243031 | 3.11 | 7.02 | 1.12 | 2.09 |
| ач • н | #231015 | >4.9 | >9 | >1.9 | >3.9 |
| Criterion H | | 5.48 | 10.97 | 2.14 | 7.29 |

Table 1 Complexity criteria

The authors have created a repository [53] containing used images for analysis, obtained images and codes.

Objective measures that were used are:

F measure (F1 score) which ranges from 0 to 100 and can be calculated [54]:

$$F = \frac{2 \times \Pr \ ecision \times \operatorname{Re} \ call}{\Pr \ ecision \times \operatorname{Re} \ call} \times 100$$
(1)

F is within the limits of $0 \le F \le 1$, ideally, F is equal to 1. The precision, also known as the positive predictive value is calculated [31]:

$$Precision = \frac{TruePositive(TP)}{TruePositive(TP) + FalsePositive(FP)}$$
(2)

while Sensitivity (Recall):

$$Sensitivity = \frac{TruePositive(TP)}{TruePositive(TP) + FalseNegative(FN)}$$
(3)

Where is TP - True Positive, pixels correctly segmented as foreground; FP - False Positive, pixels falsely segmented as foreground; TN - True Negative, pixels correctly detected as background and FN - False Negative, pixels falsely detected as background. Figure of Merit (FoM) which also ranges from 0 to 100, respectively represents the percentage value and can be calculated [55]:

$$FoM = \frac{1}{\max\{I_d, I_i\}} \sum_{k=1}^{I_d} \frac{1}{1 + \delta e^2(k)} \times 100$$
(4)

where Id is the number of points on the detected edge, and Ii is the number of points on the ideal edge, represents the distance between the detected edge and the ideal edge, and is scaling constant and is usually 1/9.

Performance Ratio (PR) which ranges from 0 to infinite [56]:

 $PR = \frac{TrueEdge(EdgePixelsIdentifiedAsEdges)}{FalseEdges(NonEdgePixelsIdentifiedAsEdges) + (EdgePixelsIdentifiedAsNon - EdgePixels)} \times 100$ (5)

Table 2 shows the Peak Signal to Noise ratio (PSNR) [49] values which show how the number of bits per pixel (BPP) is affecting image compression. It can be seen from Table 2 that the increase in BPP contributes significantly to image quality, especially with JPEG compression, when the number of image details is small. JPEG2000 and SPIHT obtained similar results, but the number of details noticeably affects the compression.

| | | | 1 | 1 | 1 | | |
|----|-----------------|------|------|------|------|------|------|
| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
| | JPEG | 28.2 | 40.3 | 52.7 | 62.2 | 61.8 | 61.8 |
| SD | JPEG2000 | 36.7 | 42.5 | 46.4 | 52.4 | 52.4 | 52.4 |
| | SPIHT | 36.6 | 42.7 | 46.6 | 53.5 | 58.5 | 70.7 |
| | JPEG | 20.7 | 26.5 | 28.9 | 31.7 | 41.5 | 56.4 |
| MD | JPEG2000 | 24.3 | 28.6 | 31.6 | 37.5 | 42.1 | 50.8 |
| | SPIHT | 24.0 | 28.4 | 31.7 | 37.5 | 42.1 | 53.9 |
| | JPEG | 19.1 | 22.8 | 24.7 | 27.6 | 28.8 | 50.4 |
| HD | JPEG2000 | 21.4 | 24.2 | 26.3 | 30.3 | 33.7 | 43.6 |
| | SPIHT | 21.3 | 24.2 | 26.1 | 30.1 | 33.6 | 43.5 |

Table 2 PSNR values for three compression algorithms with different BPP and level of details

Fig. 1, Fig. 2, and Fig. 3 show a compressed image for a different number of BPP and small number of details (SD) when using JPEG, JPEG2000, and SPIHT compression, respectively. In Fig. 4, Fig. 5 and Fig. 6, images with medium level of details compressed with JPEG, JPEG2000, and SPIHT compression and different BPP are shown, respectively. When it comes to a high number of details in an image (HD), using the JPEG, JPEG2000 and SPIHT algorithm, the resulting compressed images for different BPP are shown in Fig. 7, Fig. 8 and Fig. 9, respectively.



Figure 1 SD image with JPEG compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3

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Figure 2 SD image with JPEG2000 compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3



Figure 3 SD image with SPIHT compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3



Figure 4 MD image with JPEG compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3

From the shown figures can be seen that the quality is usable by applying all kinds of compression for all levels of detail in the image. However, degradation is greatest with a high number of details and at lower BPP, which is confirmed by results in Table 1.





Figure 5 MD image with JPEG2000 compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3



Figure 6

MD image with SPIHT compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3



Figure 7

HD image with JPEG compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3



Figure 8 HD image with JPEG2000 compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3



Figure 9 HD image with SPIHT compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3

Thus, lower BPP, compression algorithm and number of details significantly affect image quality. However, the main aim of this paper is to examine the impact of edge detection over these images, i.e. how much all of this affects the quality of the detected edge. Table 3 shows the F, FOM and PR values obtained by applying five edge detection operators over images with different level of details. Based on these results, it can be seen that the best values are obtained when the number of details in the image is small. The Roberts operator obtained the best values and the LoG the worst when the number of details in the image is small and medium, while at a high number of details, Canny obtained higher values than the others. In order to present these results visually, Fig. 10, Fig. 11 and Fig. 12 show an image with small, medium and high number of details over which edge detection was performed using five operators.



Figure 10 SD image: a) Canny, b) LoG, c) Prewitt, d) Sobel, e) Roberts





Figure 11 MD image: a) Canny, b) LoG, c) Prewitt, d) Sobel, e) Roberts



Figure 12 HD image: a) Canny, b) LoG, c) Prewitt, d) Sobel, e) Roberts

| Table 3 | |
|---------|--|
| | |

F, FOM and PR values obtained by applying different edge detectors

| | Operator | F | FOM | PR |
|----|----------|-------|-------|-------|
| | Canny | 35.11 | 89.39 | 27.54 |
| | LoG | 32.40 | 90.07 | 24.38 |
| SD | Prewitt | 35.15 | 89.40 | 26.36 |
| | Sobel | 34.07 | 89.49 | 26.31 |
| | Roberts | 46.91 | 91.74 | 44.05 |
| | Canny | 20.99 | 46.59 | 13.28 |
| | LoG | 18.90 | 57.70 | 11.65 |
| MD | Prewitt | 23.73 | 80.98 | 15.56 |
| | Sobel | 23.80 | 81.01 | 15.62 |
| | Roberts | 35.24 | 80.17 | 27.21 |
| | Canny | 22.02 | 68.94 | 14.12 |
| | LoG | 19.05 | 80.83 | 11.76 |
| HD | Prewitt | 17.98 | 63.16 | 10.96 |
| | Sobel | 18.16 | 63.75 | 11.09 |
| | Roberts | 16.88 | 56.78 | 10.15 |

3 Results

The previous section showed how these results were obtained. In Section 3, the results are divided by edge detector, i.e. a sub-section is made for each detector to make the results more transparent. The results were obtained using the mathematical models defined in Section 2. The calculation is based on the theoretical models presented in [44-47]. The results are presented in tables and for each combination of parameters (compression and edge detector) can be found in the repository [53], as well as, full size images used code.

3.1 Canny Edge Detector

Table 4, Table 5 and Table 6 show the F, FOM and PR values, respectively, obtained by applying a Canny edge detector over images with different number of details compressed by different compression algorithms. Based on the obtained results, it can be seen that by increasing the number of bits per pixel, better values are obtained. The best values are obtained when the number of details in the image is small, while when the number of details in the image is medium and high obtained values are similar.

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|----------|-------|-------|-------|-------|-------|-------|
| | JPEG | 25.55 | 32.91 | 35.47 | 35.52 | 35.49 | 35.49 |
| SD | JPEG2000 | 28.19 | 34.42 | 35.32 | 35.55 | 35.55 | 35.55 |
| | SPIHT | 28.66 | 34.05 | 35.15 | 35.52 | 35.63 | 35.56 |
| | JPEG | 17.97 | 19.49 | 20.90 | 20.51 | 20.88 | 21.04 |
| MD | JPEG2000 | 20.37 | 20.94 | 20.74 | 20.89 | 21.13 | 21.22 |
| | SPIHT | 20.63 | 20.94 | 21.18 | 21.19 | 21.36 | 21.96 |
| | JPEG | 20.45 | 20.44 | 21.94 | 21.97 | 21.90 | 22.00 |
| HD | JPEG2000 | 19.24 | 21.26 | 21.29 | 22.08 | 22.09 | 22.98 |
| | SPIHT | 19.73 | 21.12 | 21.29 | 21.83 | 22.03 | 22.11 |

Table 4 F values obtained by using a Canny edge detector

| Table | 5 |
|-------|---|
| | |

FOM values obtained by using a Canny edge detector

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|----------|-------|-------|-------|-------|-------|-------|
| | JPEG | 75.03 | 89.19 | 89.39 | 89.39 | 89.36 | 89.36 |
| SD | JPEG2000 | 86.75 | 89.30 | 89.39 | 89.36 | 89.36 | 89.36 |
| | SPIHT | 88.37 | 89.11 | 89.28 | 89.39 | 89.39 | 89.40 |
| | JPEG | 47.01 | 42.50 | 47.24 | 44.35 | 46.31 | 47.89 |
| MD | JPEG2000 | 52.63 | 47.34 | 46.30 | 46.64 | 46.96 | 47.09 |
| | SPIHT | 52.21 | 47.51 | 49.91 | 49.97 | 51.11 | 51.79 |

| HD | JPEG | 58.16 | 65.58 | 67.46 | 67.08 | 66.95 | 69.95 |
|----|-----------------|-------|-------|-------|-------|-------|-------|
| | JPEG2000 | 64.25 | 73.27 | 73.83 | 78.63 | 78.55 | 78.32 |
| | SPIHT | 55.65 | 73.91 | 75.09 | 75.13 | 75.38 | 75.65 |

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|-----------------|-------|-------|-------|-------|-------|-------|
| | JPEG | 17.16 | 24.53 | 27.49 | 27.54 | 27.51 | 27.51 |
| SD | JPEG2000 | 19.63 | 26.24 | 27.31 | 27.58 | 27.58 | 27.58 |
| | SPIHT | 20.08 | 25.82 | 27.10 | 27.55 | 27.68 | 27.59 |
| | JPEG | 10.95 | 12.10 | 13.21 | 12.90 | 13.20 | 13.32 |
| MD | JPEG2000 | 12.79 | 13.24 | 13.08 | 13.21 | 13.39 | 13.71 |
| | SPIHT | 12.99 | 13.24 | 13.44 | 13.47 | 13.52 | 13.76 |
| | JPEG | 12.85 | 12.85 | 14.06 | 14.08 | 14.02 | 14.11 |
| HD | JPEG2000 | 11.91 | 13.50 | 13.53 | 14.17 | 14.05 | 14.28 |
| | SPIHT | 12.29 | 13.38 | 13.52 | 13.96 | 14.13 | 14.21 |

Table 6 PR values obtained by using a Canny edge detector

3.2 LoG Edge Detector

Table 7, Table 8 and Table 9 show the F, FOM and PR values, respectively, obtained by applying LoG edge detectors over images with different number of details compressed by different compression algorithms. The LoG detector gave the best results when the number of details in the image is small. However, it can be seen that the values are lower when the number of details in the image is medium and high at BPP 0.1, but the values did not increase much by further increasing the BPP from 0.3 upwards.

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|----------|-------|-------|-------|-------|-------|-------|
| | JPEG | 21.46 | 31.98 | 33.07 | 32.77 | 32.72 | 32.72 |
| SD | JPEG2000 | 28.82 | 31.67 | 32.24 | 32.73 | 32.73 | 32.73 |
| | SPIHT | 29.10 | 31.89 | 32.50 | 32.77 | 32.77 | 32.84 |
| | JPEG | 16.22 | 17.99 | 18.45 | 18.55 | 18.83 | 18.89 |
| MD | JPEG2000 | 18.61 | 18.38 | 18.54 | 18.61 | 18.84 | 18.98 |
| | SPIHT | 18.49 | 18.45 | 18.51 | 18.55 | 18.98 | 18.85 |
| | JPEG | 17.78 | 18.78 | 18.99 | 19.06 | 19.08 | 19.21 |
| HD | JPEG2000 | 15.57 | 18.56 | 18.63 | 19.18 | 19.16 | 19.22 |
| | SPIHT | 16.48 | 18.26 | 18.70 | 18.86 | 18.96 | 19.04 |

Table 7 F values obtained by using a LoG edge detector

| | Tom values obtailed by using a hoo eage detector | | | | | | | |
|----|--|-------|-------|-------|-------|-------|-------|--|
| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 | |
| | JPEG | 74.29 | 89.92 | 90.11 | 90.07 | 90.72 | 90.06 | |
| SD | JPEG2000 | 89.49 | 90.02 | 90.09 | 90.09 | 90.09 | 90.09 | |
| | SPIHT | 89.25 | 90.01 | 90.02 | 90.09 | 90.08 | 90.11 | |
| | JPEG | 53.66 | 55.71 | 56.54 | 56.20 | 57.44 | 57.72 | |
| MD | JPEG2000 | 57.94 | 59.15 | 59.40 | 57.18 | 57.38 | 59.55 | |
| | SPIHT | 69.19 | 59.70 | 59.13 | 57.55 | 59.71 | 60.69 | |
| | JPEG | 78.42 | 79.42 | 80.88 | 81.50 | 81.54 | 81.86 | |
| HD | JPEG2000 | 64.75 | 77.07 | 79.16 | 80.79 | 80.80 | 80.88 | |
| | SPIHT | 64.04 | 76.20 | 79.13 | 80.10 | 80.64 | 80.82 | |

Table 8 FOM values obtained by using a LoG edge detector

PR values obtained by using a LoG edge detector

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|----------|-------|-------|-------|-------|-------|-------|
| | JPEG | 13.66 | 25.51 | 24.71 | 24.37 | 24.31 | 24.31 |
| SD | JPEG2000 | 20.25 | 23.18 | 23.79 | 24.33 | 24.33 | 24.33 |
| | SPIHT | 20.52 | 23.42 | 24.08 | 24.37 | 24.39 | 24.42 |
| | JPEG | 9.68 | 10.97 | 11.31 | 11.39 | 11.60 | 11.65 |
| MD | JPEG2000 | 11.43 | 11.26 | 11.38 | 11.42 | 11.61 | 11.76 |
| | SPIHT | 11.34 | 11.31 | 11.36 | 11.36 | 11.71 | 11.91 |
| | JPEG | 10.81 | 11.56 | 11.72 | 11.77 | 11.78 | 11.92 |
| HD | JPEG2000 | 9.22 | 11.40 | 11.45 | 11.87 | 11.77 | 11.94 |
| | SPIHT | 9.86 | 11.17 | 11.50 | 11.62 | 11.70 | 11.76 |

3.3 Sobel Edge Detector

Table 10, Table 11 and Table 12 give the F, FOM and PR values, respectively, obtained by applying a Sobel edge detector over images with different number of details compressed by different compression algorithms. Sobel detector gave good results when it comes to the small and medium number of details in the image. With high number of details, the results are poor at lower BPP.

Table 10 F values obtained by using a Sobel edge detector

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|----------|-------|-------|-------|-------|-------|-------|
| | JPEG | 20.18 | 33.95 | 34.40 | 34.29 | 34.34 | 34.34 |
| SD | JPEG2000 | 31.49 | 33.84 | 34.18 | 34.33 | 34.33 | 34.33 |
| | SPIHT | 30.99 | 33.83 | 34.42 | 34.34 | 34.41 | 34.56 |
| MD | JPEG | 17.81 | 22.61 | 23.31 | 23.75 | 23.89 | 23.77 |

| | JPEG2000 | 20.33 | 22.84 | 23.32 | 23.47 | 23.49 | 23.76 |
|----|----------|-------|-------|-------|-------|-------|-------|
| | SPIHT | 20.25 | 22.80 | 23.36 | 23.65 | 23.62 | 23.89 |
| | JPEG | 11.62 | 15.85 | 17.15 | 17.62 | 17.79 | 18.07 |
| HD | JPEG2000 | 12.88 | 17.28 | 17.65 | 18.00 | 17.98 | 18.18 |
| | SPIHT | 13.44 | 17.44 | 17.82 | 18.18 | 18.11 | 18.14 |

BPP 0.1 0.3 0.5 1 1.5 3 **JPEG** 68.69 88.86 89.32 89.47 89.50 89.50 SD **JPEG2000** 85.54 88.94 89.36 89.38 89.37 89.38 SPIHT 84.90 88.98 89.33 89.40 89.44 89.56 77.33 81.89 81.01 JPEG 68.37 79.56 80.88 MD **JPEG2000** 67.29 77.80 79.80 80.68 80.89 80.98 66.28 77.92 79.28 80.80 SPIHT 80.57 81.08 **JPEG** 48.64 57.85 60.82 62.73 64.66 63.77 HD **JPEG2000** 46.09 59.73 61.93 63.32 63.61 63.97 SPIHT 46.98 60.32 61.46 63.03 63.37 63.77

Table 11 FOM values obtained by using a Sobel edge detector

| Table 12 | | | | | | | | | | |
|---|-------|-------|-------|-------|-------|------|--|--|--|--|
| PR values obtained by using a Sobel edge detector | | | | | | | | | | |
| BPP 0.1 0.3 0.5 1 1.5 3 | | | | | | | | | | |
| JPEG | 12.64 | 25 70 | 26.22 | 26.10 | 26.15 | 26.1 | | | | |

| | DFF | 0.1 | 0.5 | 0.5 | L | 1.5 | 3 |
|----|-----------------|-------|-------|-------|-------|-------|-------|
| | JPEG | 12.64 | 25.70 | 26.22 | 26.10 | 26.15 | 26.15 |
| SD | JPEG2000 | 22.98 | 25.58 | 25.96 | 26.13 | 26.13 | 26.13 |
| | SPIHT | 22.45 | 25.56 | 26.25 | 26.15 | 26.27 | 26.29 |
| | JPEG | 10.83 | 14.61 | 15.20 | 15.58 | 15.70 | 15.59 |
| MD | JPEG2000 | 12.76 | 14.80 | 15.20 | 15.33 | 15.35 | 15.58 |
| | SPIHT | 12.69 | 14.77 | 15.24 | 15.49 | 15.57 | 15.69 |
| | JPEG | 6.58 | 9.42 | 10.35 | 10.70 | 10.82 | 11.03 |
| HD | JPEG2000 | 7.39 | 10.45 | 10.72 | 10.98 | 10.96 | 11.11 |
| | SPIHT | 7.77 | 10.56 | 10.84 | 11.11 | 11.06 | 11.09 |

3.4 Prewitt Edge Detector

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Table 13, Table 14 and Table 15 show the F, FOM and PR values, respectively, obtained by applying a Prewitt edge detector over images with different number of details compressed by different compression algorithms. The Prewitt operator obtained well values with JPEG2000 and SPIHT compression in SD images even when the number of bits per pixel is low.

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 | | |
|----|-----------------|-------|-------|-------|-------|-------|-------|--|--|
| | JPEG | 18.52 | 33.93 | 34.54 | 34.49 | 34.62 | 34.62 | | |
| SD | JPEG2000 | 31.71 | 34.10 | 31.40 | 34.50 | 34.50 | 34.52 | | |
| | SPIHT | 31.01 | 34.02 | 34.53 | 34.57 | 34.67 | 34.75 | | |
| | JPEG | 17.87 | 22.73 | 23.39 | 23.87 | 24.06 | 23.79 | | |
| MD | JPEG2000 | 20.40 | 22.91 | 23.34 | 23.66 | 23.65 | 24.02 | | |
| | SPIHT | 20.37 | 22.91 | 23.34 | 23.64 | 23.67 | 23.74 | | |
| | JPEG | 11.72 | 15.87 | 17.15 | 17.78 | 17.98 | 18.05 | | |
| HD | JPEG2000 | 12.92 | 17.39 | 17.97 | 18.05 | 18.04 | 18.15 | | |
| | SPIHT | 13.47 | 17.62 | 17.98 | 18.06 | 18.15 | 18.33 | | |

Table 13 F values obtained by using a Prewitt edge detector

Table 14

FOM values obtained by using a Prewitt edge detector

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|-----------------|-------|-------|-------|-------|-------|-------|
| | JPEG | 68.12 | 88.72 | 89.30 | 89.42 | 89.46 | 89.47 |
| SD | JPEG2000 | 85.62 | 89.09 | 89.29 | 89.36 | 89.36 | 89.36 |
| | SPIHT | 85.02 | 88.82 | 89.22 | 89.31 | 89.40 | 89.44 |
| | JPEG | 68.08 | 77.44 | 79361 | 81.68 | 80.80 | 81.03 |
| MD | JPEG2000 | 67.51 | 77.78 | 79.68 | 80.69 | 81.05 | 81.79 |
| | SPIHT | 66.56 | 77.94 | 79.18 | 80.66 | 80.72 | 80.86 |
| | JPEG | 48.76 | 57.13 | 60.49 | 62.61 | 64.00 | 64.13 |
| HD | JPEG2000 | 46.25 | 59.53 | 61.77 | 63.14 | 62.97 | 63.23 |
| | SPIHT | 47.20 | 60.28 | 61.51 | 62.89 | 62.71 | 63.25 |

| Table 15 |
|---|
| PR values obtained by using a Prewitt edge detector |

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|----------|-------|-------|-------|-------|-------|-------|
| SD | JPEG | 11.36 | 25.68 | 26.38 | 26.32 | 26.48 | 26.50 |
| | JPEG2000 | 23.21 | 25.87 | 26.22 | 26.33 | 26.33 | 26.33 |
| | SPIHT | 22.47 | 25.78 | 26.31 | 26.42 | 26.55 | 26.59 |
| | JPEG | 10.88 | 14.71 | 15.27 | 15.68 | 15.84 | 15.60 |
| MD | JPEG2000 | 12.82 | 14.86 | 15.22 | 15.50 | 15.49 | 15.88 |
| | SPIHT | 12.79 | 14.86 | 15.30 | 15.48 | 15.51 | 15.57 |
| | JPEG | 6.63 | 9.43 | 10.35 | 10.81 | 10.96 | 11.04 |
| HD | JPEG2000 | 7.42 | 10.53 | 10.95 | 11.01 | 11.00 | 11.19 |
| | SPIHT | 7.79 | 10.69 | 10.96 | 11.02 | 11.09 | 11.00 |

3.5 Roberts Edge Detector

Table 16, Table 17 and Table 18 show the F, FOM and PR values, respectively, obtained by applying Roberts edge detectors over images with different number of details compressed by different compression algorithms. When it comes to the small number of details in an image, also and mostly when the number of details in an image is medium, the Roberts operator obtained the best results using JPEG2000 and SPIHT compression.

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|-----------------|-------|-------|-------|-------|-------|-------|
| | JPEG | 20.64 | 43.98 | 46.85 | 46.64 | 46.69 | 46.69 |
| SD | JPEG2000 | 38.21 | 45.22 | 46.86 | 46.55 | 46.55 | 46.61 |
| | SPIHT | 37.63 | 45.90 | 46.70 | 46.60 | 46.73 | 46.69 |
| | JPEG | 18.42 | 31.08 | 32.71 | 33.95 | 35.03 | 35.24 |
| MD | JPEG2000 | 24.46 | 31.33 | 25.83 | 34.94 | 35.25 | 35.78 |
| | SPIHT | 24.51 | 31.36 | 34.32 | 35.01 | 35.25 | 35.42 |
| | JPEG | 12.78 | 14.06 | 14.81 | 15.11 | 14.55 | 17.05 |
| HD | JPEG2000 | 11.03 | 14.16 | 15.77 | 17.48 | 17.74 | 17.98 |
| | SPIHT | 13.47 | 17.62 | 17.98 | 18.06 | 18.15 | 18.33 |

Table 16 F values obtained by using a Roberts edge detector

| Table 17 |
|--|
| FOM values obtained by using a Roberts edge detector |

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|----------|-------|-------|-------|-------|-------|-------|
| | JPEG | 69.50 | 90.55 | 91.62 | 91.69 | 91.73 | 91.73 |
| SD | JPEG2000 | 82.01 | 90.38 | 91.59 | 91.66 | 91.66 | 91.66 |
| | SPIHT | 80.93 | 90.79 | 91.50 | 91.72 | 91.72 | 91.66 |
| | JPEG | 66.86 | 75.36 | 76.53 | 80.48 | 80.44 | 81.11 |
| MD | JPEG2000 | 58.17 | 72.75 | 79.08 | 80.21 | 80.14 | 81.01 |
| | SPIHT | 56.63 | 71.30 | 78.51 | 79.89 | 80.17 | 80.24 |
| | JPEG | 47.90 | 52.59 | 52.61 | 53.27 | 54.00 | 56.67 |
| HD | JPEG2000 | 32.82 | 45.35 | 52.80 | 57.17 | 58.30 | 59.94 |
| | SPIHT | 47.20 | 60.28 | 61.51 | 62.89 | 62.71 | 63.25 |

Table 18

PR values obtained by using a Roberts edge detector

| | BPP | 0.1 | 0.3 | 0.5 | 1 | 1.5 | 3 |
|----|----------|-------|-------|-------|-------|-------|-------|
| SD | JPEG | 13.01 | 39.55 | 44.07 | 43.70 | 43.79 | 43.79 |
| | JPEG2000 | 30.92 | 41.27 | 44.09 | 43.54 | 43.54 | 43.54 |
| | SPIHT | 30.16 | 42.42 | 43.81 | 43.64 | 43.76 | 43.61 |
| MD | JPEG | 11.29 | 22.55 | 24.31 | 25.70 | 26.96 | 27.21 |

| | JPEG2000 | 16.19 | 22.81 | 25.83 | 26.85 | 27.22 | 27.46 |
|----|-----------------|-------|-------|-------|-------|-------|-------|
| | SPIHT | 16.23 | 22.84 | 26.13 | 26.94 | 27.22 | 27.29 |
| | JPEG | 7.33 | 8.18 | 8.69 | 8.90 | 8.51 | 10.27 |
| HD | JPEG2000 | 6.20 | 8.25 | 9.36 | 10.59 | 10.79 | 10.88 |
| | SPIHT | 7.79 | 10.69 | 10.96 | 11.02 | 11.09 | 11.11 |

In Section 2 it could be seen visually and objectively how compression and different BPP values effect on quality of images. While in Section 3, edge detection was performed on these images, and based on the results presented in tables by all operators, the effect of compression on edge detection can be seen. BPP effect on edge detection as well as the number of details in an image. The Canny operator has proven to be a good solution but when the number of details in the image is small or medium, the Roberts operator finds its application. For this reason, Figure 13 shows the edge detection using the Roberts operator. Detection is shown for an image that is compressed with JPEG technique at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3.



Figure 13

Roberts detection for SD image with JPEG compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3

Since the Canny operator proved to be a very good solution when the number of details in the image is high even at lower BPP values, Figure 14 shows the edge detection using this operator. Detection is shown for an image that is compressed with JPEG technique at BPP a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3.



Figure 14 Canny detection for HD image with JPEG compression at BPP: a) 0.1, b) 0.3, c) 0.5, d) 1, e) 1.5, f) 3

Thus, Figure 13 and Figure 14 are only a visual representation of the results obtained in Section 3. All images for the results obtained can be found in the repository [53].

Conclusions

This paper analyzes gradient (Sobel, Prewitt, Robert), Laplacian of Gaussian and Canny operator. Operators were applied to images which consist different number of details (small, medium and high) and compressed by JPEG, JPEG2000 and SPIHT compression algorithms at different bits per pixel. Objective measures were used - F measure, FOM and PR and the results are tabulated.

Based on the obtained results, it can be concluded that when the number of details in the image is small and medium and when using JPEG compression, the best results are obtained using the Roberts operator, only at a BPP of 0.1 Canny achieved better values. Other operators have similar values. With the same amount of detail in image, JPEG2000 and SPIHT compression achieve better results than JPEG, which is reflected in edge detection. Also, the Roberts operator obtained the best results over the other operators, however, the values are similar to JPEG compression except when the BPP is low. Using high detail images and JPEG, JPEG2000 and SPIHT compression, the best edge detection was obtained with the Canny operator. Edge detection is better when JPEG2000 and SPIHT are used.

The results obtained in this paper contribute to the further development of image compression algorithms to be more suitable for use in systems where image processing such as segmentation and edge detection is used. However, it provides an incentive to optimize edge detectors for image compression at lower bits per pixel values, with consideration of the complexity of the image.

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